Proposed problem to Mathematical Reflections

Evaluate

$$\int_0^{\frac{\pi}{2}} \frac{1 - \ln \cos x}{x^2 + (1 - \ln \cos x)^2} dx$$